



Examination Answer Books

12 Pages

Instructions to Candidates

1. Please give the information requested in the boxes below.
2. Enter your name in the space provided to the right, fold over and seal down (using the label provided) to hide your name.
3. The answers must be legibly written. The Examiners can either ignore illegible script or have it typed and the expense of typing charged to the candidate.
4. Write your answers in ink.
5. Begin each answer on a fresh page. Do all rough work in the answer book and cross it through.
6. No part of this book is to be torn out; it must be handed in complete.
7. If more books than one are used, fasten them together using the tags available from the invigilator(s).
8. Every book must be handed in. In no circumstances may answer books, used or unused, be taken out of the examination venue.

Complete, fold and seal
(see note 2 below)

SURNAME:

Davies

FORENAME(S):

Lloyd William

1	Student Number	1707513/1
2	Title of Examination Paper	Mathematics (Test 2)
3	Module Code	GGAC0006
4	Date and Time of Examination	11 MAY 2018
5	Examination Venue	Main hall GCS
6	Seat Number	15
7	Number of Answer Books handed in	1

List the numbers of the questions you have attempted	Office Use
1	
3	
Q1	
a	14
b	0
c	0
d	7
Q3	
a	4
b	1
c	5
d	0
e	1
f	3
Total	35/80

Test 2

43.75

3 a) i) $z_1 = 5+3j$ and $z_2 = 2-7j$

$$= (5+3j) + (2-7j)$$

$$= \underline{7-4j} \quad \checkmark \text{ ①}$$

ii) $z_1 - z_2$

$$= (5+3j) - (2-7j)$$

$$= \underline{3-4j} \quad \times$$

iii) $\frac{5+3j}{2-7j} \times \frac{2-7j}{2+7j} = \frac{(5+3j)(2-7j)}{(2-7j)(2+7j)}$

$$= \underline{10-35j+6j-21j^2}$$

$$= \underline{31-29j} \quad \times$$

iv) $(z_1)^2 \times (z_2)$

$$\cancel{5+3j} (5+3j)(5+3j)$$

$$= 25 + 15j + 15j + 9j^2$$

$$z_1^2 = 16 + 30j \quad \checkmark \text{ ①}$$

$$(16+30j)(2-7j)$$

$$32 - 112j + 60j - 210j^2 \quad \checkmark$$

$$= \underline{242 - 52j} \quad \checkmark \text{ ①}$$

Q3

4
✓

b) $12x^2 + 7 = -5x$
 $12x^2 + 5x + 7 = 0$

quadratic formula ~~is~~ $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$x = \frac{-5 \pm \sqrt{5^2 - 4 \times 12 \times 7}}{2 \times 12}$ ✓ ①

~~is~~

$$c) i) (5 + 7j)^6$$

A

$$r = \sqrt{5^2 + 7^2}$$

$$r = 8.60 \checkmark \textcircled{1}$$

$$\theta = \tan^{-1} \left(\frac{7}{5} \right)$$

$$= 54.46^\circ \checkmark \textcircled{1}$$

$$= 8.6^6 (\cos(6 \times 54.46) + j \sin(6 \times 54.46)) \checkmark \textcircled{1}$$

$$= 404567.23 (\cos(326.76) + j \sin(326.76))$$

$$= 404567.23 (0.84 + 0.55j)$$

$$= 339836.47 + 222511.98j \checkmark \textcircled{1}$$

5
✓

$$ii) (-1 + 3j)^5$$

$$r = \sqrt{(-1)^2 + 3^2}$$

$$r = 2.83 \checkmark$$

$$\theta = \tan^{-1} - \frac{3}{1}$$

$$= -71.56^\circ \dots$$

$$= -71.57^\circ$$

$$= 2.83^5 (\cos(5 \times -71.57) + j \sin(5 \times -71.57))$$

$$= 181.52 (\cos(357.85) + j \sin(357.85))$$

$$= 181.52 (1 + (-0.037j))$$

$$= 181.52 + (-6.72j) \checkmark$$

d)

x

0
✓

$$e) 5 - 3j \text{ conjugate } = 5 + 3j \checkmark \textcircled{1}$$

1
✓

$$f) z_1 = 2 + 3j \quad z_2 = 3 - 6j \quad z_3 = -1 + j$$

$$\begin{aligned} &= (2 + 3j)(3 - 6j)(-1 + j) \\ &= (6 - 12j + 9j - 18j^2)(-1 + j) \quad \checkmark \quad \textcircled{1} \\ &= (24 - 3j)(-1 + j) \quad \checkmark \quad \textcircled{1} \\ &= -24 + 24j + 3j - 3j^2 \\ &= \underline{-21 + 27j} \quad \checkmark \quad \textcircled{1} \end{aligned}$$

3

1 a) i)

$$AB = \begin{pmatrix} 3 & -2 & -3 \\ 5 & 4 & 1 \\ 2 & 3 & 4 \end{pmatrix} \begin{pmatrix} 2 & -1 & 4 \\ 8 & 7 & 3 \\ -5 & 0 & 1 \end{pmatrix}$$

$$AB = \begin{pmatrix} 6 & -18 & 15 \\ 37 & 33 & 33 \\ 8 & 23 & 21 \end{pmatrix} \quad \checkmark \textcircled{5}$$

1st row

$$(3 \times 2) + (-2 \times 8) + (-3 \times -5) = 5 \quad \checkmark$$

$$(3 \times 1) + (-2 \times 7) + (-3 \times 0) = 3 + (-14) + 0 = -11 \quad \checkmark$$

$$(3 \times 4) + (-2 \times 3) + (-3 \times 1) = 12 + (-6) + -3 = 3 \quad \checkmark$$

2nd row

$$(5 \times 2) + (4 \times 8) + (1 \times -5) = 10 + 32 + (-5) = 37 \quad \checkmark$$

$$(5 \times 1) + (4 \times 7) + (1 \times 0) = 5 + 28 + 0 = 33 \quad \checkmark$$

$$(5 \times 4) + (4 \times 3) + (1 \times 1) = 20 + 12 + 1 = 33 \quad \checkmark$$

3rd

$$(2 \times 2) + (3 \times 8) + (4 \times -5) = 4 + 24 + (-20) = 8 \quad \checkmark$$

$$(2 \times 1) + (3 \times 7) + (4 \times 0) = 2 + 21 + 0 = 23 \quad \checkmark$$

$$(2 \times 4) + (3 \times 3) + (4 \times 1) = 8 + 9 + 4 = 21 \quad \checkmark$$

ii)

$$BA =$$

1st

$$(2 \times 3) + (1 \times 5) + (4 \times 2)$$

$$2 \times 3$$

$$2 \times 2$$

ii) $B \times A$

$$\begin{pmatrix} 2 & 1 & 4 \\ 8 & 7 & 3 \\ -5 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 3 & -2 & -3 \\ 5 & 4 & 1 \\ 2 & 3 & 4 \end{pmatrix}$$

1st

$$(2 \times 3) + (1 \times 5) + (4 \times 2) = 6 + 5 + 8 = 19 \quad \checkmark$$

$$(2 \times -2) + (1 \times 4) + (4 \times 3) = -4 + 4 + 12 = 12 \quad \checkmark$$

$$(2 \times -3) + (1 \times 1) + (4 \times 4) = -6 + 1 + 16 = 11 \quad \checkmark$$

2nd

$$(8 \times 3) + (7 \times 5) + (3 \times 2) = 24 + 35 + 6 = 65 \quad \checkmark$$

$$(8 \times -2) + (7 \times 4) + (3 \times 3) = -16 + 28 + 9 = 21 \quad \checkmark$$

$$(8 \times -3) + (7 \times 1) + (3 \times 4) = -24 + 7 + 12 = -5 \quad \checkmark$$

4
✓

3rd

$$(-5 \times 3) + 0 + (1 \times 2) = -15 + 2 = -13 \quad \checkmark$$

$$(-5 \times -2) + 0 + (1 \times 3) = -15 + 3 = -12 \quad \times$$

$$(-5 \times -3) + 0 + (1 \times 4) = -15 + 4 = -11 \quad \times$$

$$BA = \begin{pmatrix} 19 & 12 & 11 \\ 65 & 21 & -5 \\ -13 & -12 & -11 \end{pmatrix}$$

③

iii) Not possible $\times$ iv) Not possible $\checkmark$ ①



v) $|A| =$

$$\begin{vmatrix} 3 & -2 & 3 \\ 5 & 4 & 5 \\ 2 & 3 & 4 \end{vmatrix}$$

$-24 + 9 + (-40) = -55$ (2)

$-1 + 55 = 54$ ✓

~~55~~

α

$48 + (-4) + (-45) = -1$ ✓

5/5

vi) $|B| =$

$$\begin{vmatrix} 2 & 1 & 4 \\ 8 & 7 & 3 \\ -5 & 0 & 1 \end{vmatrix}$$

$-140 + 0 + 8 = -132$ ✓ (1)

$13 + 132 = 145$ ✓

$14 + (-1) + 10 = 23$ ✓

~~13~~ ✓

5/5 ✓

vii) $A+B = \begin{pmatrix} 5 & -1 & 1 \\ 13 & 11 & 4 \\ -3 & 3 & 5 \end{pmatrix}$ ✓ (1)

viii) Not possible as both have to be squares (1) ✓

b) ?

c) ?

$$d) \begin{cases} 3x + 2y - z = 17 \\ 2x - y + 4z = -5 \\ 5x - y - z = 6 \end{cases}$$

$$D = \begin{vmatrix} 3 & 2 & -1 \\ 2 & -1 & 4 \\ 5 & -1 & -1 \end{vmatrix}$$

$10 + (-1)(-5) - 5(-6) = 5 + (-12) + 30 = 23$
 $47 + 5 - 58 = -6$
 $3 + 40 + 4 = 47$
 $47 + 5 - 58 = -6$
 $Top = 5 + (-12) + 30 = 23$
 $bottom = 3 + 40 + 4 = 47$

$$D_1 = \begin{vmatrix} 17 & 2 & -1 \\ -5 & -1 & 4 \\ 6 & -1 & -1 \end{vmatrix}$$

$6 + (-68) + 10 = -52$
 $60 + 52 = 112$
 $17 + 48 + (-5) = 60$
 $45 + 11 = 56$

$$D_2 = \begin{vmatrix} 3 & 17 & -1 \\ 2 & -5 & 4 \\ 5 & 6 & -1 \end{vmatrix}$$

$25 + 72 + (-34) = 63$
 $343 - 63 = 280$
 $15 + 340 + (-12) = 343$

$$D_3 = \begin{vmatrix} 3 & 2 & 17 \\ 2 & -1 & -5 \\ 5 & -1 & 6 \end{vmatrix}$$

$-85 + 15 + 24 = -46$
 $-102 - 124 - 520 = -746$
 $(+18) + (-50) + (-34) = -66$

$$x = \frac{D_1}{D} = \frac{112}{56} = x = 2$$

$$y = \frac{D_2}{D} = \frac{280}{56} = y = 5$$

$$z = \frac{D_3}{D} = \frac{-56}{56} = z = -1$$